# Controls on the deformation of the central and southern Andes (10–35°S): Insight from thin-sheet numerical modelling

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# Abstract

What mechanisms and conditions formed the central Andean orocline and the neighbouring Altiplano plateau? Why does deformation decrease going from the central to the southern Andes? To answer these questions, we present a new thin-sheet model that incorporates three key features of subduction orogenesis: (1) significant temporal and spatial changes in the strength of the continental lithosphere in the upper plate; (2) variable interplate coupling along a weak subduction channel with effectively anisotropic mechanical properties; and (3) channelled flow of partially molten lower crust in the thickened upper plate.

Application of this model to the present kinematic situation between the Nazca and South American plates indicates that the deformed Andean lithosphere is significantly weaker than the undeformed South American foreland, and that channel flow of partially melted lower crust smoothes topographic relief. This channel flow is, therefore, inferred to control intra-orogenic topography and is primarily responsible for the development of the Andean plateau since the Miocene.

A parameter study shows that the decrease in shortening rates from the central to the southern Andes can be attributed to the weakening of the orogenic Andean lithosphere and to along-strike variations in interplate coupling within the subduction zone. The current rates of deformation are reproduced in the model if: the Andean lithosphere is assumed to be 5-15 times weaker than the lithosphere of the Brazilian shield; interplate coupling is assumed to be relatively weak, such that the subduction zone in the vicinity of the central Andes is some 10-20 times weaker than the Andean lithosphere; and coupling itself decreases laterally by some 2-5 times going from the central to the southern Andes.

# 1. Introduction

The bend of the Andes, known as the Bolivian orocline (Fig. 1), is a first-order structure visible from space. Oroclinal bending in the Andes was originally proposed by Carey (1958) to have involved anticlockwise rotation of the Andes north of the Arica bend (Fig. 1) superposed on an initially straight Andean chain. Indeed, palaeomagnetic studies have revealed a consistent and roughly symmetrical pattern of anticlockwise rotations north of the Arica bend and of clockwise rotations south of it (e.g. MacFadden et al., 1995). Today, however, there is consensus that the central Andes were never entirely straight (Sheffels, 1995) and that the original curvature of the plate margin was enhanced during Andean orogenesis rather than having been imposed later (Isacks, 1988).

Here, we refer to the segment of the Central Andes containing the Andean plateau as the central Andes (lower case in "central"), reaching from ~ 16°S to 25°S. Parts of Andes south of this latitude to the southern limit of our model we term the southern Andes. Our subdivision differs from the traditional division of the Andean chain into Central and Southern Andes at ~ 30°S (Gansser, 1973), and reflects the north-to-south change in morphology and rates of deformation, as discussed throughout this paper.

Several explanations have been given for the development of the Bolivian orocline. Isacks (1988) and Allmendinger et al. (1997) argued that the bending resulted from differential shortening along the Andean chain, with shortening increasing towards the Arica bend. Kley et al. (1999) have shown how oroclinal bending could have been achieved by differential shortening. In their model, several fault-bounded blocks underwent various degrees of displacement and differential rotation. Shortening estimates require that rotation of the limbs of the orocline did not exceed 5-10°. Riller and Oncken (2003) also related oroclinal bending to orogen-parallel gradients in horizontal shortening plus block rotations and strike-slip movements. These authors linked these movements to the orogen-normal growth of the central Andean plateaus.

Numerical models of Liu et al. (2002) and Yang et al. (2003) set boundary conditions at the western margin of the South America that effectively prescribe the evolution of this margin and preclude modelling the bending of the orocline. Yanez and Cembrano (2004) used a thin sheet approximation model to show that along-strike variations in coupling between Nazca and South American plates can result in bending of the western boundary of the Central Andes. Sobolev et al. (this volume) uses a model that incorporates laws of empirical flow and a coupled thermomechanical approach to compare the evolution of the central and southern Andes, yet the application of their two-dimensional (2D) modelling to the problem of oroclinal

bending, effectively a three-dimensional (3D) process, should be tested using a 3D approach sometime in future. Here, we present a complementary approach to that of Sobolev et al. (this volume) by considering a map view of deformational processes in the Andes.

As noted above, the Bolivian orocline is spatially related to another primary structure, the central Andean Altiplano-Puna plateau, which , following the Tibetan plateau, is the second largest plateau on Earth (Fig. 1). The thick crust underlying the plateau (>70 km, James, 1971; Wigger et al., 1994; Zandt et al., 1994; Giese et al., 1999; Yuan et al., 2000) is mainly attributed to crustal shortening (Isacks 1988). There are differences between the Altiplano and Puna parts of the plateau: The Puna is slightly higher and has greater relief than the Altiplano. Moreover, the lithosphere is thicker beneath the central and eastern parts of the Altiplano (70-80 km), but less thick (60-70 km) beneath the westernmost Altiplano and Puna (Whitman et al., 1992).

In a synthesis of space-geodetic measurements, Neogene shortening data, and palaeomagnetic data, Lamb (2000) has shown that the Altiplano is currently growing eastwards (see also Oncken et al., this volume; Sobolev et al., this volume) without significant uplift of the plateau (in contrast to the results of Yang et al., 2003). Numerical models of orogenesis that incorporate plateau evolution attribute the relatively low relief in the central part of the Himalayan and Andean chains to the lateral flow of weak, possibly partially molten, rock in a middle to lower crustal channel within the thickened orogenic crust (Beaumont et al., 2001, 2004; Vanderhaeghe et al., 2003; Royden, 1996; Shen et al., 2001).

Channel flow is driven by differential pressure associated with topographic gradients, such that highly mobile, viscous crust flows from beneath areas of greater to lesser elevation. In flattening topographic gradients, channel flow can form orogenic plateaux as shown in a number of numerical experiments (e.g., Shen et al., 2001; Husson and Sempere, 2003; Medvedev and Beaumont, in press). Thermal conditions beneath the Altiplano plateau favour partial melting (Springer, 1999; Springer and Förster, 1998; Brasse et al., 2002; Babeyko et al., 2002) and therefore makes channel flow a viable mechanism for the formation of the Andean plateaux, as already proposed by Husson and Sempere (2003) and Gerbault et al. (2005).

The change in style and in the amount of deformation along the Andean orogenic belt also requires explanation. Deformation of the central Andes exceeds that in the southern Andes, as manifest by progressive southward narrowing of the 3 km elevation contour on the map (Fig. 1) and by the higher average elevation of the central Andes. The southward decrease in shortening is accompanied by an increase in crustal thickness to 70 km or more in the central Andes.

Present shortening rates averaged over last several million years show a similar north-south trend: the central Andes are currently shortening at rates of 1 - 1.5 cm/y (see Oncken et al., this volume, and discussion within), while in the southern Andes the rates are so low (<0.5 cm/y) as to be difficult to estimate (Kley and Monaldi, 1998). Several workers attribute this variation in shortening and shortening rates to along-strike differences in the degree of coupling between the Nazca and South American plates (Lamb & Davis, 2003; Yanez and Cembrano, 2004; Sobolev et al., this volume; Hoffmann-Rothe et al., this volume), possibly induced by latitudinal, climate-induced variations in erosion rates and the mechanical properties of the trench fill as well as the age and strength of the oceanic plate.

To better understand these first-order deformational features of the Andes, we developed and applied a new numerical model that incorporates some of the salient, physical features of subduction orogenesis. We employ a backward-modelling approach; i.e., we incorporate data on the recent kinematic, gravitational and thermal states of the South America–Nazca plate boundary system together with knowledge of the current bathymetry, topography and rheology from geophysical studies to back-calculate the local rates of shortening, thickening and rotation in the upper plate.

These calculations are mechanism-specific; they combine lateral shortening, topography and channel flow. The values obtained for primary orogenic features (e.g., orogenic geometry in map view, lithospheric thickness, rotation rates) are then compared with the available data on current rates of shortening (from geological estimations) and rotation (from palaeomagnetic studies) to gain insight into the driving mechanisms and parameters controlling Andean orogenesis. Therefore, the criterion for judging the relative importance of different mechanisms is the degree to which predicted, back-calculated values match current, measured values.

We emphasize that our model is not intended to simulate Andean orogenesis or even to provide a detailed picture of Andean orogenic evolution. Rather, it is a vehicle for conducting a series of experiments and parameter studies, each of which is designed to test the plausibility of various mechanisms proposed for the first-order Andean features described above. From a methodological standpoint, our approach is similar to that adopted by Lithgow-Bertelloni and Guynn (2001) to predict stress field variations over the entire Earth. However, our model deals with a much smaller region and is tailored to account for the specific characteristics of recent Andean subduction orogenesis. The numerical basis of our model (thin viscous sheet approximation), of course, limits our analysis precluding analysis of faulting and thrusting processis.

In the next section, we present details of our mechanical model, including the rheologies of the oceanic lower plate, the continental upper plate and the interplate subduction channel, as well as the way in which we have adapted the thin-sheet approach to examine the proposed orogenic processes. We then present a basic model relevant to Andean orogenesis and analyse how changing model parameters affect Andean deformation, particularly deformation related to the formation of the Bolivian orocline and the Andean plateau.

## 2. Thin-sheet approximation applied to Nazca-South American subduction orogenesis

The thin-sheet approximation of England and McKenzie (1982) involved determining the balance of stresses in continental lithosphere subjected to tectonic forces exerted by an undeformable, indenting plate (in their case, Asia and India, respectively). The continental lithosphere was assumed to be a uniform sheet that is not subjected to any basal traction, and whose width and breadth far exceed its thickness. England and McKenzie (1982) suggested that the strain rate of the continental lithosphere does not vary vertically, and that a balance of vertically integrated stresses can approximate the balance of stresses in the lithosphere. Thus, simple 2D equations can be used to approximate the 3D deformation of the continental lithosphere. To apply this general approach to the Nazca-South American subduction orogeny, we have had to make some modifications, as outlined below.

Firstly, we consider the deformation of two plates (Nazca and South America) rather than of just a single indented plate, as in England and McKenzie's (1982) original approach. The Nazca and South American plates have different characteristics and deformational states: Whereas the western part of the South American continent comprises the Andes and is highly deformed, the Nazca plate is oceanic and virtually undeformed (Fig. 1). The lower plate is, therefore, inferred to be stronger than the upper continental plate.

Subduction of the Nazca plate beneath South America precludes direct application of the thin-sheet approximation in its classical formulation because the lower plate imposes a basal traction on the overlying continental lithosphere in the vicinity of the subduction zone. This poses a problem because simply introducing additional force into the thin-sheet force balance (e.g., Husson and Ricard, 2004) is not compatible with the principle assumption of no basal traction in the thin-sheet approximation (England and McKenzie, 1982). We therefore treat the plates' interface as a separate mechanical entity, our so-called "subduction zone", which comprises a thin channel of un- or partly consolidated sediments and their metamorphosed equivalents sandwiched between adjacent parts of the upper and lower plates (Fig. 2).

The rocks within this channel, known as the subduction channel (Peacock, 1987; Cloos and Shreve, 1988a,b; Hoffmann-Rothe et al., this volume), are intrinsically weak, the more so if they are subjected to high pore-fluid pressure, as is reasonably expected for subducting oceanic sediments undergoing prograde metamorphic dehydration (e.g., Hacker et al., 2003). These weakening agents are inferred to reduce overall coupling between the upper and lower plates. Thus, the vertically integrated strength of the subduction zone is not only a function of the strengths of the oceanic and continental plates, but also of the dip and strength of the subduction channel. In the Andean case, the subduction channel is assumed to have the same inclination as that of the oceanic slab, dipping 15-30° to the east within the 20-50 km depth interval. This depth interval coincides with the depth interval of seismic coupling (Isacks, 1988; Hoffmann-Rothe et al., this volume).

For the general purposes of our model, the upper, South American plate is assumed to comprise a weak Andean orogenic belt and a stronger orogenic foreland. In making this simple assumption, we purposefully ignore evidence that the South American plate is more complex, with at least two foreland domains (Brazilian shield and basement arches of the Sierras Pampeanas; Kley at al., 1999; Sobolev et al., this volume) and with variations in thickness and thermal properties along the strike of the Andes (e.g., differences between Altiplano and Puna lithospheres, Whitman et al., 1992; Kay et al., 1994). Significant though these differences may seem, they turn out to be small in comparison to the truly large differences between the Andean chain and its foreland.

The assumption that the Andean lithosphere is weaker than its foreland lithosphere is based on several studies indicating that the lithosphere under high-elevated Andes is thinner (e.g., Whitman et al., 1992; Kay et al., 1994) and hotter (Henry and Pollack, 1988; Springer and Förster, 1998; Springer 1999) than the lithosphere under undeformed parts of South America (east from Andes). This is especially true for the Puna part of the plateau. The modest deformation of the Andean foreland (east from the orogenic chain, Fig. 1) is also a qualitative indication that it is stronger than the orogenic lithosphere.

The existence of weak, mid to lower crust is another property of the Andes that cannot be modelled with the classical thin-sheet approximation. England and McKenzie's (1982) formulation assumes uniform deformation throughout the continental lithosphere. However, this is unreasonable for the Andes in light of

abundant seismic (Swenson et al., 2000; Yuan et al., 2000; Haberland and Rietbrock, 2001) and magnetotelluric (Brasse, 2002; Haberland et al., 2003) evidence for partial melting (Babeyko et al., 2002; Zandt et al., 2003) in the lower crust beneath the plateau regions. Experimental studies indicate that even minute ( $\leq 0.1$  volume %) amounts of partial melt can reduce rock strength by several orders of magnitude (Rosenberg and Handy, 2005). Therefore, the partially molten, lower Andean crust is reasonably assumed to be highly mobile, resulting in channel flow (Husson and Sempere, 2003; Yang et al., 2003; Gerbault et al., 2005) and non-uniform deformation of the Andean lithosphere.

The parameters listed in Table 1 reflect these Andean characteristics and account for the following basic observations mentioned in the introduction:

- (1) A shortening rate for the central Andes of 1 1.75 cm/y and for the southern Andes of 0 0.5 cm/y; this corresponds to a difference in shortening rates between centre and south of at least 0.9 cm/y.
- (2) Ongoing oroclinal bending of the Andes.
- (3) Orogen-normal, eastward growth of the Andean plateau in the absence of increasing altitude.

The plate motion rates in Figure 1 are with respect to the mid-Atlantic ridge (Silver et al., 1998). If we assume that the undeformed Andean foreland is moving westwards at a rate of 3 cm/y, then shortening of the Andes accommodates only part of this plate motion, while the other part is taken up by the westward motion of the western margin of the South American continent. Because shortening rates decrease from the central to southern parts of the orogen, the motion of the western boundary of South America must decrease accordingly. The slower westward advancement of the central Andes results in bending of the plate boundary and development of the Bolivian orocline. Thus, our model automatically fulfils condition 2 if condition 1 is satisfied. The mechanism of bending described above is similar to that proposed by Isaacks (1988).

#### 3. Model characteristics

We modified the classical thin-sheet approximation of England and McKenzie (1982) by using the higher order, asymptotic analysis of Medvedev and Podladchikov (1999 a, b). Our analysis shows that although the balance of forces presented in England and McKenzie (1982) are applicable to our problem, the kinematic model must be modified to account for mid to lower crustal flow beneath the Andean plateau (Appendix A; England and McKenzie, 1982; Medvedev and Podladchikov, 1999a). This results in the following equations that relate force balance to the thickness and density of the lithosphere:

$$2\frac{\partial \overline{\tau}_{xx}}{\partial x} + \frac{\partial \overline{\tau}_{yy}}{\partial x} + \frac{\partial \overline{\tau}_{xy}}{\partial y} = g\Phi\rho H \frac{\partial H}{\partial x}$$

$$\frac{\partial \overline{\tau}_{xx}}{\partial y} + 2\frac{\partial \overline{\tau}_{yy}}{\partial y} + \frac{\partial \overline{\tau}_{xy}}{\partial x} = g\Phi\rho H \frac{\partial H}{\partial y}$$
<sup>(1)</sup>

where  $\tau$  is a deviatoric stress tensor, *H* is the thickness of the crust with density  $\rho$ ,  $\Phi = (1 - \rho/\rho_m)$  is the buoyancy amplification factor, and  $\rho_m$  is the density of the mantle lithosphere. The overbar stands for integration over the depth of the lithosphere. Equation 1 assumes no traction at the base of the lithosphere and lithostatic approximation for pressure. The lithosphere is regarded as a viscous fluid, such that the integrated stresses relate to strain rates in the following way:

$$\overline{\tau} = 2\overline{\mu}\dot{\varepsilon}$$
$$\dot{\varepsilon}_{ij} = (\partial V_i / \partial x_j + \partial V_j / \partial x_i) / 2$$
<sup>(2)</sup>

where only the horizontal components of stress and strain rate are considered:  $\{x_b, y_j\} = \{x, y\}$  are the horizontal coordinates, and  $\{V_b, V_j\} = \{V_x, V_y\}$  are the depth-invariant horizontal velocities. In the following subsections, we discuss, in some detail, the parameters of the rheological relation in equation 2, as well as the deformational processes in the system. The model system is divided into three main types of lithosphere: oceanic, continental, and transitional (the subduction zone).

# 3.1. Oceanic Lithosphere

The strength of the oceanic plate depends on its thermal state, which, in turn, is a function of its age (Turcotte and Schubert, 1982). Therefore, we adopt the following relation:

$$\overline{\mu}_{o} = \mu_{o} L_{o} \sqrt{age/(average\_age)}$$
(3)

where  $\mu_o$  is the characteristic viscosity of the oceanic plate and  $L_o$  is the characteristic thickness of the plate. The *average\_age* in this equation is calculated from the 26 to 50 My age range of the oceanic crust in this area (Fig. 1, Müller et al., 1993). This results in age-dependent variations in the strength of the oceanic plate (eq. 3) of up to a factor of two (Table 1).

# **3.2. Subduction zone elements**

The subduction zone elements (Fig. 2) comprise layers of oceanic and continental lithosphere, and the subduction channel (Peacock, 1987; Cloos and Shreve, 1988a,b). This composite structure requires a detailed analysis to complete the integrated rheological relation in equation 2. We therefore consider stresses associated with each component of the strain-rate tensor in Appendix B and show that the rheological relation in equation 2, as applied to the subduction zone, can be expressed as:

$$\begin{pmatrix} \overline{\tau}_{xx} \\ \overline{\tau}_{yy} \\ \overline{\tau}_{xy} \end{pmatrix} = 2L_s \begin{bmatrix} \mu_{xx} & 0 & 0 \\ 0 & \mu_{yy} & 0 \\ 0 & 0 & \mu_{xy} \end{bmatrix} \bullet \begin{pmatrix} \dot{\varepsilon}_{xx} \\ \dot{\varepsilon}_{yy} \\ \dot{\varepsilon}_{xy} \end{pmatrix} (4)$$

where  $L_s$  is the characteristic thickness of the lithosphere in the subduction zone, and  $\mu_{yy}$ ,  $\mu_{xx}$ , and  $\mu_{xy}$  are viscosities of the subduction zone in the directions of consideration. Note that the thin-sheet approximation used in our study relates the stresses integrated over the depth of the lithosphere to the average strain rate of the lithosphere. Thus, equation 4 considers only horizontal directions, with the X axis oriented east-west and the Y axis north-south.

Appendix B lists the constituent properties of the subduction zone elements. These properties are based on poorly known parameters (e.g. the thickness and viscosity of the subduction channel). Therefore, equation 4 uses only the most general constraints in Appendix B regarding the anisotropic stiffness of the subduction zone elements. We assume  $\mu_{yy} > \mu_{xx} > \mu_{xy}$  in our reference model (Table 1).

# 3.3. Continental lithosphere

The integrated strength of continental lithosphere strongly depends on the thermal state and thickness of the lithosphere (England and McKenzie, 1982; Ranalli, 1995). However, data on the Earth's thermal field is sparse and South America is no exception. We have, therefore, tried to find some empirical dependence for the strength of the lithosphere on a temperature-dependent parameter that can be easily extracted from available data sets.

To understand variations in the strength of the continental lithosphere, we compared the integrated strength of the lithosphere before and after deformation (Fig. 3a). Sudden, uniform thickening of the lithosphere (Fig. 3b, dashed line) results in thickening of the strong crustal and upper-mantle layers and, therefore, in a significant increase of integrated strength. Integrated strength of the lithosphere increases less significant if thickening is gradual. Thermal relaxation and radioactive heating increase average temperature of the lithosphere and make it weaker (Fig. 3 b, solid line). Applied to Andes, however, this mechanism is proved to be insignificant (model 1 of Babeyko et al., 2002).

Geophysical evidence for detachment of the lithospheric mantle beneath parts of the Andean plateau (e.g., Yuan et al., 2000) lends credence to the idea that lithospheric weakening is triggered by the upwelling of hot, asthenospheric mantle. The weakening associated with this heat advection from below supersedes the initial strengthening associated with lithospheric thickening. Thus, the contraction of the lithosphere can result in its significant weakening (Dewey, 1988; Kay et al., 1994; Babeyko et al., this volume; Sobolev et al., this volume).

A reliable measure of the amount of deformation in the lithosphere is the thickness of the crust. Weakening associated with orogenic thickening is assumed to have affected the entire part of South America considered in our study. Despite the fact that the Andean foreland crust is thinner than the Andean orogenic crust ( $H_0 < H^*$ ), it is much stronger and more viscous. Thus, we relate the integrated strength of the continental lithosphere to the thickness of crust with the following empirical relation (Fig. 4):

$$\overline{\mu}_{c} = \begin{cases} \mu_{c0}L_{c} & (H < H_{0}) \\ \mu_{c0}L_{c} \exp(b(H - H_{0})^{2}) & (H_{0} < H < H^{*}) \\ \mu_{c1}L_{c} & (H > H^{*}) \end{cases}$$
(5)

where  $\mu_{c0}$  and  $L_c$  are the characteristic viscosity and thickness of the continental lithosphere, respectively, and the coefficient  $b = \log(\mu_{c1} / \mu_{c0})/(H_0 - H^*)^2$  is chosen to ensure that viscosity varies continuously from  $\mu_{c0}$  to  $\mu_{c1}$  as a function of crustal thickness, *H*. Thus, the changes of rheology, in equation 4, not only represent changes owing to increased heat advection during thickening, but also to the direct effects of thickening of the orogenic lithosphere.

The thickness of the thickened continental crust,  $H^*$ , is chosen to be 62 km for all the models. This is less than the maximum observed value of 70 km and corresponds to the critical thickness of crust required to drive channel flow, as discussed and estimated in the next section. Thus, the most important rheological parameter of the continental crust is the viscous strength ratio of the orogenic and foreland lithospheres,  $\overline{\mu}_{c1}/\overline{\mu}_{c0} = \mu_{c1}/\mu_{c0}$ . This ratio is 0.04 in the reference model (Fig. 4), meaning that the orogenic Andes are 25 times weaker than the Andean foreland. In a separate analysis, we tested different values of this ratio, including situations where the orogenic lithosphere is assumed to be stronger than the foreland  $(\overline{\mu}_{c1}/\overline{\mu}_{c0}>1)$ .

We note that the viscosity distribution in our model is similar to the integrated effective viscosities in the models of Sobolev et al. (this volume; circles and reference model in Fig. 4), but that the drop in the integrated viscosity of our reference model is greater than in their model. The 2D models of the central Andes orogeny in Sobolev et al. (this volume) suggest a higher ratio  $\overline{\mu}_{c1}/\overline{\mu}_{c0}$  (0.1) than in our reference model (0.04), as discussed below.

Our model integrates the properties of the continental lithosphere with depth (Fig. 5), but, in reality, the strength of the continental lithosphere varies unevenly with depth (Fig. 3). Strong layers in the upper crust and lithospheric mantle sandwich a weak, mid to lower crustal layer. Appendix A shows that although the contribution of the weak, lower crustal layer to force balance may be insignificant, this layer contributes significantly to the kinematics of continental deformation.

# 3.4. Channel flow and the orogenic plateau

We distinguish three types of orogenic processes (Fig. 6). The Nazca plate opposes the westward motion of the South American continent, creating lateral compressional forces,  $F_t$ , that lead to shortening in the Andes (Fig. 6b). We term this process "tectonic thickening". The thickened lithosphere is subjected to a second process, gravity spreading, i.e., deformation of the lithosphere under the force of gravity and buoyancy,  $F_g$  (Fig. 6c). Tectonic and gravitational forces,  $F_t$  and  $F_g$ , are the most important forces acting on the lithosphere, as they are responsible for most deformation in the system. Most of thin-sheet approximations applied to model large orogenic systems took into account these two main mechanisms (e.g., England and McKenzie, 1982; Yanez and Cembrano, 2004), and the equation 1 in our model balances the integrated stresses caused by these forces.

In Appendix A we consider a third mechanism when analysing deformation of the continental crust: channel flow in the mid to lower crust (Fig. 6d). The importance of channel flow within orogenic continental crust has been discussed extensively in the literature (e.g. Beaumont et al., 2001, 2004; Royden, 1996; Clark and Royden, 2000; Shen et al, 2001, Gerbault, 2005) as being a requisite for development of orogenic plateaus (Royden, 1996; Vanderhaeghe et al. 2003; Husson and Sempere, 2003). The classical thin-sheet approach (England and McKenzie, 1982) was developed before channel flow was considered, so that thin-sheet models developed, so far, have not reproduced the topographical features of orogenic plateaus (England and Houseman, 1988).

The force  $F_c$  associated with the channel flow is a result of variations of lithostatic loads at the base of thickened continental crust. Differential load of upper crust results in the flow and corresponding drug by the low viscosity channel material on the more competent parts of the lithosphere. This drug is insufficient to contribute to the integrated balance of forces ( $F_c << F_g$  and  $Fc << F_t$ , Fig. 3c, Appendix A), but potential contribution of the channel flow to the kinematics of orogenesis is significant. The following equation describes the evolution of the crustal thickness accounting for both, bulk deformation of the crust and the channel flow (Appendix A):

$$\frac{\partial H}{\partial t} + \left(\frac{\partial V_x H}{\partial x} + \frac{\partial V_y H}{\partial y}\right) - \frac{\rho g h_c^3}{12\mu_{ch}} \left(\frac{\partial^2 S}{\partial x^2} + \frac{\partial^2 S}{\partial y^2}\right) = 0 \quad (6)$$

where  $V_x$  and  $V_y$  are the horizontal velocities obtained from the solution of equations 1 to 5. The second bracketed term corresponds to flow in the lower crustal channel and *S* is the elevation of topography with respect to sea level (Appendix A, parameters listed in Table 1). The influence of the channel increases significantly when the material in the channel becomes very weak during partial melting. Medvedev and Beaumont (in press) show that a decrease of viscosity to  $\mu_{ch} = \mu_p \approx 10^{18} - 10^{20}$  Pa·s is sufficient to establish a plateau above the channel. Note, that eq. 6 is used in our model to evaluate the rates of thickness changes ( $\partial H/\partial$ ), but we do not consider finite-time evolution of the model. Variations of viscosity in the channel are represented in the model by the relation:

$$\mu_{ch} = \begin{cases} \mu_p & (H < H^*) \\ \mu_t & (H > H^*) \end{cases}$$
(7)

The viscosity in the crustal channel not directly beneath the plateau,  $\mu_t = 10^{22}$  Pa·s, was chosen to render the influence of the channel in these regions insignificant. The condition for the transition  $\mu_{ch} = \mu_p$  $\rightarrow \mu_{ch} = \mu_t \ (H=H^*)$  should be consistent with the geometry of the orogen. In particular, the tip of the lowviscosity channel should coincide with the edge of the flat part of the orogen. We term a channel with this configuration a "geometrically consistent channel" (GCC, Fig. 7a). If the tip of the channel extends beyond the edge of a plateau, termed an "overdeveloped channel" (OC, Fig. 7a), the flux of weak, partially molten rock is too high to support the overlying plateau, and the plateau collapses. Alternatively, if the channel is too short, an "underdeveloped channel" (UC, Fig. 7a), the plateau never becomes flat during shortening, and the margins of the plateau are characterized by high topographic gradients. Of course, the geometry of the Andean orogenic plateau is not as simple as in our experimental model (Fig. 7a) and a direct estimation of  $H^*$ is impossible for the Andes.

To specify the condition for a geometrically consistent channel, we consider channel flux for different transitional positions in our experimental model (Figs. 7a, b). An estimate of the average flux in the channel for all possible transitions (Fig. 7c) shows that the change from a transient to a stable flux occurs where the channel has exactly the same lateral extent as the overlying plateau (point GCC, Fig. 7c). An absolute value for the flux of low viscosity material in the channel can be calculated for the central Andes with the following equation (see also Appendix A):

1/

$$\left|q_{c}\right| = \sqrt{q_{cx}^{2} + q_{cy}^{2}} = \frac{\rho g h_{c}^{3}}{12\mu_{ch}(H^{*})} \left[ \left(\frac{\partial S}{\partial x}\right)^{2} + \left(\frac{\partial S}{\partial y}\right)^{2} \right]^{\frac{1}{2}}$$
(8)

The absolute value of the flux depends on two parameters: the elevation, *S*, and the critical crustal thickness,  $H^*$ . Figure 8 presents our calculated average fluxes in low-viscosity channel for different critical thicknesses using actual elevation data from the considered domain of South America (Fig. 1). The results in Figure 8 compare well with our analytical predictions (Fig. 7) and yield a critical thickness value for Andean crust of  $H^* = 62$  km. This corresponds to a plateau elevation of 3.5 km. We use these parameters in our numerical models.

Equation 8 clearly relates the intensity of the channel flow with variations of topography, because the terms in brackets characterise the absolute value of topographic gradient. Results on Fig. 8 show that high-elevated Andes (with crustal thickness > 57 km) average topographic gradient decreases with increase of elevation and reaches stable minimal value at 3.5 km elevation (H=62 km). Thus, the results in Figure 8 indicate that the Andes are typically flatter at elevations exceeding 3.5 km.

## 3.5. The numerical model

The MATLAB code developed for this study is based on the finite element method (Kwon and Bang, 1997). The code uses data regarding the topography and bathymetry (termed *S*), the age of the ocean floor, and the plate boundary from the SFB267 database (http://userpage.fu-berlin.de/~data/Welcome.html). Then, the topographic data is converted into crustal thicknesses by using an Airy isostatic model,  $H=H_0+S/\Phi$  (Turcotte and Schubert, 1982). To evaluate unknown initial (undeformed) thickness of the continental crust,

 $H_0$ , and isostatic amplification factor,  $\Phi$ , we used estimations of crustal thickness fromGötze and Kirchner (1997) and Kirchner et al. (1996). Finally, the code separates the region in question into three parts: oceanic plate, continental plate, and a 100 km wide subduction zone. Table 1 lists the parameters of the reference model.

The system of equations 1 to 7 was solved using the finite-element approximation based on a second-order interpolation inside the elements. The calculations were performed on a serial PC with a grid of up to  $120 \times 100$  elements (up to  $360 \times 300$  integrating points). The model was designed so that the density of the finite-element grid is a parameter. We used that parameter to test the robustness of the numerical model by comparing results based on the fine and coarse grids.

The boundary conditions for equation 1 are eastward motion of the Nazca plate at 5 cm/y along its western boundary, westward motion of the Brazilian shield at 3 cm/y along its eastern boundary, and free-slip along the northern and southern boundaries of the model. In the reference model, we ignore the oblique motion of the Nazca plate by assuming that the northward component of oblique motion can cause local effects along the plate margins, for example, coast-parallel motion and faulting in the South American western fore-arc. We assume, however, that these effects do not significantly affect the general pattern of deformation at the scale of the Andes (Hoffmann-Rothe et al., this volume).

#### 4. Results and Discussion

## 4.1. The reference model

In this section, we present the results of a reference model that employs the parameters listed in Table 1. These parameters were chosen to help us understand the development of primary Andean features, such as the modestly deforming southern Andes, the bending of the Bolivian orocline, and the development of the Andean plateau. The model is not designed to match the observations completely. Rather, the goal is to demonstrate that the processes considered above are physically possible given the geodynamic and rheological constraints on Andean orogenesis.

The reference model does not present a unique solution. Analysing the series of numerical experiments based on different sets of parameters, we chose our reference model (Table 1) to illustrate typical results. We discuss variations of parameters in the following sections.

Figure 9 illustrates the rates of thickness change, particularly how the three processes considered above (Fig. 6) act to change the thickness of the Andean crust. The rate of tectonic thickening (Fig. 9a) can be evaluated by eliminating gravity (e.g., by setting the density of the crust to 0 in eqs. 1 and 7). As expected, the weaker, orogenic parts of the South American plate accommodate most of the tectonic thickening in this case. The main factor controlling the rate and distribution of tectonic thickening is the relative integrated strengths of the continental plate, the subduction zone, and the oceanic plate (Fig. 5, Table 1). Weak orogenic lithosphere, therefore, favours faster, more localized and pronounced thickening in the upper plate, whereas stronger orogenic lithosphere engenders a broader zone of thickening.

The amount and rate of gravitational spreading associated with existing topographic gradients can be evaluated by setting the boundary velocities to 0 (Fig. 9d). The main parameter characterizing the rate and distribution of gravity spreading is the strength of the continental plate with respect to the magnitude of the gravity forces acting on the plate surface. Accordingly, a narrow, weak and heavy upper plate favours faster, and more widely distributed, gravitational spreading than a broad, strong, and light upper plate.

The rate of thickness change in the upper plate owing to channel flow was evaluated by setting the bulk velocities in equation 6 to  $V_x=0$  and  $V_y=0$  (in this case the kinematic update, eq. 6, becomes independent from the system eqs 1–5). The influence of the crustal channel is recognisable only in orogenic lithosphere directly beneath the area within 3 km elevation line, where it flattens the topographic relief to a plateau-like morphology. This thickness change rate is heterogeneous, with thinner patches being thickened, and areas of greater thickness becoming somewhat thinner. This smoothing of topography is ascribed to channel flow of partially molten rock. For example, heterogeneous relief of Puna results in uneven distribution rates of thickening, whereas flat topography of the central Altiplano do not result in significant channel flow and in associated thickness changes (cf. Fig. 1).

Figure 9d presents rates of thickness changes accounting for all three considered mechanisms. The rate of thickening within 3 km elevation line is heterogeneous, tracking the influence of channel flow discussed in the paragraph above. The important feature of the total rate of thickness changes is the active thickening of the crust in the vicinity of the 3 km elevation line. As thickening progresses, the 3 km elevation line expands, tracking the lateral expansion of the Andes. Note, that our numerical model is designed to estimate rates of thickening, not to calculate long-term evolution of Andes. Thus, the conclusion about lateral expansion of Andes illustrated by Fig. 9d is valid only for the recent state of the Andean orogeny.

Figure 10a indicates that the faster westward advancement of the southern Andes (2.5 cm/y from 30– 35 °S) than of the central Andes (1–1.5 cm/y from 15–20°S) is consistent with the observed bend of the Bolivian orocline. The shortening rate of the Andes in the model (Fig. 10b) is equal to the rate at which the foreland approaches the western boundary of the South American plate. In the model, all of this convergence is accommodated by the deformation of the orogenic lithosphere. The shortening rate varies strongly along strike of the Andean chain, from up to 1.5 cm/y at 15–20° S (in agreement with Oncken et al., this volume) to less than 0.5 cm/y in the southern Andes.

# 4.2. 3D aspects of the thin-sheet model

The model used to obtain the results above incorporates an analysis of the horizontal thin sheet with distributed properties, such as integrated viscosity. Similar results within the limits of current accuracy can be obtained by using a series of east-west, cross-sectional models (e.g., Husson and Ricard, 2004). The advantage of our model lies in its ability to predict the distribution of some of the 3D features of the Andean orogeny, such as strike-parallel flow of material, and rotations of parts of the Andean crust.

Figure 11a depicts the north-south flow of crustal material in the Andes. The flow is presented by an equivalent velocity field for a normalised, 40 km thick crust. Thus, a 3 mm/y velocity along the southern border of the Puna plateau represents flow of the normalized, 40 km thick crust at this rate. This significant mass flow must be accounted for when restoring the deformation of the Andes, as already shown by Gerbault et al (2005).

Figure 11b shows a clockwise rotation of the southern part of the Andes and an anti-clockwise rotation of the northern part, consistent with field and palaeomagnetic observations (Isacks, 1988; Butler et al., 1995; Hindle and Kley, 2002; Riller and Oncken, 2003; Rousse et al., 2002, 2003). These vorticity values correspond to rotations of 1.5–2.2 degrees per million years, which is comparable to the estimates of Rousse et al. (2003) and Riller and Oncken (2003). The least rotation occurs in the central Andes between 20 and 24°S, in agreement with results showing that most rotation in this region occurred earlier, during the Palaeogene (Arriagada et al., 2003).

Another 3D aspect of our model is that the properties of the subduction zone can be depth integrated (Appendix B). We performed a sensitivity analysis in order to examine the influence of effective mechanical anisotropy of the subduction elements on Andean-type orogenesis. We did this by varying the viscosity parameters in equation 5. The reference model (Table 1) is based on the relation  $\mu_{yy} >> \mu_{xx} >> \mu_{xy}$ . Changing this relationship to  $\mu_{xx} \approx \mu_{xy}$  or  $\mu_{xx} \approx \mu_{xy}$  and tuning rheology to have reasonable results for central and southern parts of our model results in the domination of gravity spreading over tectonic thickening in the Peruvian and Bolivian Andes. This scenario is unrealistic, suggesting that the assumption made in our reference model of subduction zone elements with strongly directional mechanical properties is quite reasonable. This is confirmed by calculations in Appendix B (where it is shown that  $\mu_{yy}$  is of order of  $\mu_c$ , or even stronger; and that  $\mu_{xx} >> \mu_{xy}$ ) and depicted by the ratios in the grey-shaded domains of Figures 12 and 13 (for which  $\mu_c >> \mu_{xx}$ , see next section). Thus, our analytical investigations (Appendix B) and numerical experiments (next section) supports the relation of the reference model,  $\mu_{yy} >> \mu_{xx} >> \mu_{xy}$ .

# 4.3. Formation of the Bolivian orocline and shortening of the Andes

In this section, we search for parameter values that are consistent with the observed amount and rates of shortening and rotation in the Andes. A series of numerical experiments revealed that the main parameters responsible for oroclinal bending and differential shortening of the Andes are the viscosity ratios  $\overline{\mu}_{c1}/\overline{\mu}_{c0}$  and  $\overline{\mu}_{xx}/\overline{\mu}_{c1}$  (Fig. 12). The ratio  $\overline{\mu}_{c1}/\overline{\mu}_{c0}$  (Fig. 4) determines the degree to which the orogenic lithosphere weakens as the crust thickens, as well as the degree to which the orogenic lithosphere is weaker than the foreland lithosphere. The ratio  $\overline{\mu}_{xx}/\overline{\mu}_{c1}$  (Fig. 5a) is the strength contrast between the orogenic Andean lithosphere and the subduction zone in the direction of subduction. Figure 12 depicts the results of 400 numerical experiments conducted to determine which strength ratios are consistent with observed amounts and rates of deformation, all other parameters being held constant at the values listed in Table 1. The results show, for example, that the orogenic Andean lithosphere must be at least 14 times weaker than the foreland lithosphere ( $\overline{\mu}_{c1}/\overline{\mu}_{c0} < 0.07$ , Fig. 12) for the model to match the observed deformation. Otherwise, the difference in shortening rates between the central and southern Andes is too low, or the deformation of the southern Andes is too high.

The calculations used to obtain the results in Figure 12 involve no strike-parallel changes in the rheology of the subduction zone. However, several workers (Yanez and Cembrano, 2004; Lamb and Davis, 2003; Sobolev et al., this volume; Hoffmann-Rothe et al., this volume) emphasize that in the central Andes

the coupling between the upper and lower plates and, therefore, the subduction zone in between are stronger than to the south.

To test the influence of lateral variations in subduction zone rheology, we ran a series of experiments in which the strength of the subduction zone,  $\overline{\mu}_{xx}$ , decreased linearly away from the central Andes (19°S), both to the north and the south. The measure of this change,  $R_{c/s}$ , is defined as the ratio of  $\overline{\mu}_{xx}$  at 19°S and at 32°S (in the southern Andes). Figure 13 presents results for  $R_{c/s} = 1$ , 2, and 5. To fit the observed shortening rates in the Andes, models with  $R_{c/s} > 1$  require less weakening of the orogenic lithosphere (i.e. smaller values for ratio  $\overline{\mu}_{c1} / \overline{\mu}_{c0}$ ) than the reference model with  $R_{c/s} = 1$ . We note that weakening of the orogenic lithosphere, ratio  $\overline{\mu}_{c1} / \overline{\mu}_{c0}$ , in our reference model is several times greater than that predicted by Sobolev et al. (this volume), as shown in Figure 4. However, we obtain comparable values of weakening if we use  $R_{c/s} > 1$ , as shown in Figure 13.

Models with an along-strike variation in strength contrast of  $R_{c/s} > 1$  can be considered as a combination of two end-member models. In one (our reference model), the weakening of the Andean orogenic lithosphere compared to the foreland lithosphere is the prime cause of along-strike variations in Andean shortening and oroclinal bending. This model also faithfully reproduces the observed coincidence of accelerating Andean shortening and decelerating convergence between the Nazca and South American plates (Hindle et al., 2002) during the most recent 10 My. This requires weakening of the orogenic lithosphere by a factor of more than 15, and can only be obtained by assuming unrealistic rheologies or thermal fields. In comparison, the fully numerical cross sectional models in Sobolev et al. (this volume) exhibit weakening by no more than a factor of 10.

In the other end-member model, the kinematics of Andean orogenesis are primarily determined by a systematic, along-strike change in the degree of coupling between the Nazca and South American plates. The importance of that property of the Andean orogeny was outlined in a number of works (Isacks, 1988; Lamb and Davis, 2003; Yanez and Cembrano, 2004; Sobolev et al., this volume). This explains the initiation of oroclinal bending in the absence of orogenic structures along the western side of South America. But without meeting the condition that the orogenic lithosphere is weaker than forelednd, the Andes cannot develop any further and the deformation of South America will be well distributed. Figure 13 indicates that if  $\overline{\mu}_{c1} / \overline{\mu}_{c0} \sim 1$ 

or higher, the Brazilian shield will be actively deforming.

Both end-member models have advantages and disadvantages in explaining the salient features of Andean orogenesis, so it is not surprising that reality is best explained by a combination of these endmembers. A model in which the strength of the thickened Andean lithosphere decreases by only 5-10 times (Fig. 13) and the strength of the subduction zone decreases from the central to the southern Andes by a factor of 2-5 yields shortening rates that are consistent with observed Recent values.

# 4.4 Comparison with previous models

Thickening of the lithosphere yields significant weakening according to equation 5 (Fig. 4). As mentioned above, this weakening is responsible for the formation of the Bolivian orocline and the Andean plateau, and also explains the modest shortening of the southern Andes in our reference model. This contrasts with the analogue model of Marques and Cobbold (2002), in which the thickened continental lithosphere becomes a strong crustal indentor that effects oroclinal bending. In later stages, this indentor is incorporated into the Andean plateau. The Andean plateau develops because the proto-plateau is stronger than the foreland, according to conclusion of Marques and Cobbold (2002) model.

Numerical experiments in which lithospheric strength increases with crustal thickness ( $\overline{\mu}_{c1} / \overline{\mu}_{c0} >$  1) exhibit deformation of the entire Brazilian shield comparable or even higher than deformation of Andes (Fig. 13), which, of course, is entirely unrealistic. The underlying cause of the discrepancy between the results of our reference model (with its requirement that  $\overline{\mu}_{c1} / \overline{\mu}_{c0} <$ 1) and the Marques and Cobbold (2002)

model (2002,  $\overline{\mu}_{c1}/\overline{\mu}_{c0}>1$ ) is the different conditions at the base of the model: in the analogue experiments of Marques and Cobbold (2002), deformation is influenced by the friction along the base of the box, and therefore cannot propagate far from the indentor. In contrast, the base of our numerical model is frictionless (emulating a low-viscosity asthenosphere at the base of the model lithosphere), allowing deformation to propagate far into the upper continental plate, where the weak orogenic lithosphere accommodates most of the shortening.

Channel flow of partially molten rock beneath the high Andes is responsible for flattening of the Andean plateaux. Without this mechanism, the Andes would thicken continuously in the centre instead of

growing laterally by thickening at the plateau margins (Lamb, 2000; Sobolev et al., this volume). The model of Liu et al. (2002) and Yang et al. (2003) shows continuous and nearly uniform uplift of the Andes because the impenetrable boundary in that model is set just outside the Andes, precluding any flow exterior to the these mountains and, therefore, precluding lateral expansion of the Andes. We should note that the models of Liu et al. (2002) and Yang et al. (2003) demonstrated clearly the importance of low-crustal flow in the formation of flat topography of the Andean plateaus.

The age-dependent strength of the oceanic plate (eq. 3) does not significantly influence the pattern of deformation in the Andes in our reference model. This is inconsistent with the results of Yanez and Cembrano's (2004) model in which the age of the subducting Nazca plate was deemed to be one of the major factors responsible for the development of the Bolivian orocline. In assessing this discrepancy, we point out that the oceanic plate plays a very different role in the two models.

In Yanez and Cembrano's (2004) model, the age of the oceanic lithosphere is used only to estimate the degree of coupling between the undeformable, oceanic, lower plate and the deformable, continental, upper plate The older and colder the oceanic plate, the greater the degree of interplate coupling. In our model, however, the oceanic plate is strong but deformable, and the interaction between the oceanic and continental plates is specified along their contact within the subduction zone. If we were to relate the properties of the subduction zone to the age of the subducting oceanic plate (e.g., by a special value of the parameter  $R_{c/s}$ ), the distribution of deformation in our model would probably also depend on the age of the oceanic plate.

#### **5.** Conclusions

We present a new numerical thin-sheet model to analyse the recent state of deformation in the Andean orogen. Our numerical experiments show that several first-order features of the Central and Southern Andes can be explain by three aspects which we incorporate as novel features of our model: the effective mechanical anisotropy of the subduction zone, the distribution of integrated strength of the upper continental plate, and channelled flow of partially molten rock at the base of the thickened crust within this upper plate.

Special analysis shows that the subduction zone behaves anysotropically depicting the influence of weak subduction channel and corresponding weakness in the direction of subduction. The degree of that weakness measures the coupling between the Nazca and South American plates. We also assume that the strength of continental lithosphere depends on the thickness of the crust. Thus, our model enabled us to assess the relative importance of interplate coupling and strength of the orogenic lithosphere with respect to the foreland lithosphere. The validity of the models was determined by their ability to reproduce observed, Recent shortening rates across the Andes.

For uniform coupling between the Nazca and South American plates, realistic shortening rates were obtained only when the orogenic lithosphere was 20-100 times weaker than the foreland lithosphere. For coupling between the plates that varies along strike of the trench (i.e., from north to south), we found that southward reduction of interplate coupling eases the requirement for strong weakening of the orogenic lithosphere of Andes. Thus, models with calculated shortening rates that are consistent with currently measured rates involve a decrease in interplate coupling by a factor of 2 to 5 from the central to the southern Andes, and a decrease in the strength ratio of Andean orogenic lithosphere to Andean foreland by a factor of only 5 to10.

The incorporation of a channel of weak, probably partially molten, middle crust in the upper plate of the model subduction orogen reduces topographic relief in the overlying crust and provides a simple mechanism for the development of the Andean plateau. The weak crust forms a cushion which flattens the orogen and allows the orogenic plateau to grow laterally, as observed in the Andes today. We ascertain that channel flow is active beneath parts of Andes with an altitude greater than 3.5 km.

Numerical experiments allow us to constrain the rheological parameters associated with presently observed variations in shortening and vorticity along the Andean chain. These variations are also reflected in the measured rates of bending of the Bolivian orocline.

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# Appendix A. Stress and mass balance in the thin viscous sheet approach

In this section we derive the governing equations of the thin viscous sheet and assess the validity of the simplifications related to this approach. Here, we analyse only a specific 2D case, as the general theory of the thin-sheet approximation is presented in Medvedev and Podladchikov (1999 a and b). The force balance in terms of stresses is:

$$\frac{\partial \sigma_{zz}}{\partial x} + 2 \frac{\partial \tau_{xx}}{\partial x} + \frac{\partial \tau_{xz}}{\partial z} = 0$$
(A1)  
$$\partial \tau_{zz} = \partial \sigma_{zz}$$

$$\frac{\partial \partial x_{xz}}{\partial x} + \frac{\partial \partial z_{zz}}{\partial z} = \rho g \quad (A2)$$

where  $\sigma$  is the full stress tensor and  $\tau$  is the deviatoric part of the stress tensor. We use an equality which results from mass conservation and viscous rheology  $(\tau_{xx} + \tau_{zz} = \mu(\varepsilon_{xx} + \varepsilon_{zz})=0)$ , and thus pressure  $p=-\tau_{zz} - \sigma_{zz}$ =  $\tau_{xx} - \sigma_{zz}$ ). Integration of equation A1 over the depth of the lithosphere yields (Medvedev and Podladchikov, 1999a):

$$\frac{\partial \overline{\sigma}_{zz}}{\partial x} + 2 \frac{\partial \overline{\tau}_{xx}}{\partial x} = 0$$
(A3)

where we use the condition of zero traction on the top and at the base of the lithosphere. The overbars refer to integration over the thickness of the lithosphere. Double integration of equation A2 over the lithospheric depth gives:

$$\overline{\sigma}_{zz} = R_z H + \overline{\overline{\rho}} g - \iint_L \frac{\partial \tau_{xz}}{\partial x} dz dz$$
(A4)

where  $R_z$  is the pressure at the compensation depth and double overbar stands for double integration. The rheology is:

$$\tau_{xz} = \mu \left( \frac{\partial v_x}{\partial z} + \frac{\partial v_z}{\partial x} \right)$$
(A5)

and therefore the distribution of the horizontal velocity is:

$$v_{x}(x,z) = V_{x}(x) + \int_{-L}^{z} \left(\frac{\tau_{xz}}{\mu} - \frac{\partial v_{z}}{\partial x}\right) dz$$
 (A6)

where  $V_x$  is the velocity at the base of the lithosphere, z=-L, and  $v_z$  is vertical velocity.

Equations A1 - A6 are exact (not approximated) equations for depth integration in the lithosphere (Medvedev and Podladchikov, 1999a). The only simplifying assumption made in that system of equations is that the lithosphere behaves as incompressible viscous fluid.

England and McKenzie (1982) simplified these equations by making two assumptions: (i) they ignored shear stress in equation A4,  $\tau_{xz}=0$ ; and (ii) they ignored velocity variations in equation A6 and set  $v_x=V_x$ . After substitution of the shortened equations A4 and A6, the governing equation A3 becomes:

$$4\frac{\partial}{\partial x}\left(\overline{\mu}\frac{\partial V_x}{\partial x}\right) = g\Phi\rho H\frac{\partial H}{\partial x}$$
(A7)

where *H* is the thickness of the crust with density  $\rho$ ,  $\Phi = (1 - \rho/\rho_m)$  is the buoyancy amplification factor, and  $\rho_m$  is the density of the mantle lithosphere.

Simplifications (i) and (ii) in England and McKenzie (1982) are justified for a thin sheet with a nearly even strength distribution and subjected to no friction at the top and bottom boundaries. Oceanic lithosphere fulfils these conditions adequately. However, they are not valid for continental lithosphere characterized by significant strength variations (Fig. 3). Whereas the weak part of the mantle lithosphere (bounded at the base by  $\tau_{xz}=0$ ) should not exert any significant shear stress, the strong variations in strength owing to partial melting in the lower crust can result in finite shear stresses.

There is no way of estimating exactly the influence of this shear stress, so we must make some simplifying assumptions. Here, we ease conditions (i) and (ii) by assuming that the shear stress  $\tau_{xz}$  is small, thus rendering the vertical stress in equation A4 close to the lithostatic pressure.

The velocity distribution (eq. A6) can change in the lower crustal channel, especially if partial melting occurs (Fig. 3c). Hence, we assume the total velocity to be:

$$v_x = V_x + v_c$$
(A8)

where  $v_c$  is the velocity in the lower crustal channel. This velocity has a finite value within the channel and is zero outside of it. Note that this perturbation of velocity in the lower crustal channel does not significantly change the normal stress in equation A3, as in the following equation:

$$\overline{\tau}_{xx} = 2\overline{\mu}\frac{\partial V_x}{\partial x} + 2\int_h \mu_{ch}\frac{\partial v_c}{\partial x}dz \approx 2\overline{\mu}\frac{\partial V_x}{\partial x}$$
(A9)

This is because  $\mu_{ch}$  is much smaller than the average viscosity of the continental lithosphere. The integral in equation A9 is taken over the thickness of the low-viscosity channel in the lower crust, *h*. Thus, equation A7

describes the stress balance for the lithosphere for conditions that are not as restrictive as in England and McKenzie (1982).

Although the velocity correction in equation A8 does not change the balance of integrated stresses in the thin sheet, it is significant enough to change both the balance of masses and the changes in crustal thickness. These changes are described with the equation:

$$\frac{\partial H}{\partial t} + \frac{\partial q_x}{\partial x} = 0$$
(A10)
$$q_x = q_{xV} + q_{xV}$$

where  $q_{xV} = (V_x H)$  is the flux corresponding to the bulk velocity,  $V_x$ , and  $q_{xv}$  is the flux corresponding to the additional flow in the lower crustal channel. We adopted a simplified approach to the estimations of the flux,  $q_{xv}$  (Clark and Royden, 2000), in which the channel of constant thickness,  $h_c$ , occupies the entire width of the continental crust. The flux is then described by:

$$q_{xv} = -\frac{\rho g h_c^3}{12\mu_{ch}} \frac{\partial S}{\partial x}$$
(A11)

where S is the elevation of the continent. Medvedev and Beaumont (in press) show that the viscosity distribution,  $\mu_c$ , should decrease significantly at the edges of the plateau, such that  $\mu_c = \mu_p$  beneath the plateau. Otherwise,  $\mu_{ch} = \mu_t \gg \mu_p$ , assuming that partial melting in the lower crust is responsible for the development of the plateau. Medvedev and Beaumont (in press) show that orogens with a 10 km thick channel can acquire a plateau-like geometry if  $\mu_p \sim 10^{18} \cdot 10^{20}$  Pa·s, and  $\mu_t \ge 25 \mu_p$ . Here we associate that rheological transition with a critical thickness of the crust,  $H^*$ :

$$\mu_{ch} = \begin{cases} \mu_p & (H < H^*) \\ \mu_t & (H > H^*) \end{cases}$$

An appropriate value for  $H^*$  is discussed in the main part of the text. 1D->2D!!!

We analysed here the classical thin-sheet approach and show that the 3D analogue of equation A7 (England and McKenzie, 1982) can describe the evolution of the two main parts of our model: the Nazca and South American plates (see eqs 1-2). The 3D analogue of kinematic update (eqs A10-A11) can be easily obtained by adding y-related component of flux into eq. A10:

$$\frac{\partial H}{\partial t} + \frac{\partial q_x}{\partial x} + \frac{\partial q_y}{\partial y} = 0$$

where estimation of  $q_y$  can be obtained the same way as for  $q_x$ , simply replacing subscripts and differentiations from x to y. Equation A7 does not apply to the subduction zone and is considered in more detail in the text and in Appendix B.

# Appendix B. Rheological properties of the subduction zone elements

The subduction zone elements (Fig. 2) include layers of oceanic and continental lithosphere, and the subduction channel. The complicated geometry of the subduction zone requires a detailed analysis of the depth integration. We therefore consider the stresses associated with each component of strain-rate tensor. Even though the subduction zone consists of several elements in the east-west direction (Fig. 2), we analyse the entire zone and assume average values for strains and related stresses across it. The following derivations present an approximate analysis aimed mainly at understanding the general characteristics of the thin-sheet representation of the subduction zone. The approximate analysis of this appendix ignores difference between thickness of the subduction zone lithosphere,  $L_s$ , its width, D, and length of the subduction channel, l. We understand that these parameters can be different by several times, but we limit our analysis to the qualitative analysis distinguishing only parameters that differ by orders of magnitude. We leave the quantitative estimations of the parameters of the subduction zone to the numerical experiments.

In our analysis, we assume the continental and oceanic crust to be much stronger than the rocks in the subduction channel (Sobolev et al., this volume). This assumption allows us to ignore deformation in the continental and oceanic parts of the subduction zone elements, and to concentrate on stresses associated with deformation of the subduction channel only. We also assume that the length of the subduction channel, l, is greater than its thickness, h, and introduce the channel aspect ratio,  $\Delta = l/h >> 1$  (Fig. B1 b).

Consider stresses associated with variations in the east-west velocity,  $V_x$ , and in the east-west direction, X (Fig. B1a). Those variations represent the xx term of the strain-rate tensor,  $\dot{\varepsilon}_{xx} = \partial V_x / \partial x \approx V_x / D$  (D is the width of the subduction zone). The total variations of velocity can be broken down into two components: channel-parallel and channel-normal,  $V_x = V_\tau + V_n$  (Fig. B1b). The channel-parallel velocity induces Couette flow (Fig. B1c), whereas channel-normal velocity squeezes the channel, inducing Poiseuille flow (Fig. B1d). The average stresses associated with the two components of  $V_x$  are:

$$\sigma_{\tau} = \mu_s V_{\tau} / h$$
$$\sigma_n = 2\mu_s V_n l^2 / h^3$$

where  $\mu_s$  is the viscosity of the rock in the subduction channel. The first equation is a standard expression of the shear stress associated with Couette flow (e.g., Turcotte and Schubert, 1982). The second equation represents the average pressure from the channel response on the channel-perpendicular squeezing. Depth-integration yields the shear and normal stresses on the subduction channel:

$$\overline{\sigma}_{\tau} = \Delta \mu_s V_x$$
$$\overline{\sigma}_n = 2\Delta^3 \mu_s V_x$$

In these expressions, we assume an undeformable continental lithosphere in the presence of the weak subduction channel, rendering  $V_x$  to be invariant with depth. The stress associated with motion parallel to the channel boundaries,  $\sigma_{\tau}$ , is much smaller than  $\sigma_n$ . Thus, the stress-strain-rate relationship for the *xx* component of deviational stress can be approximated as:

$$\overline{\tau}_{xx} \approx \overline{\sigma}_n = 2\Delta^3 D \mu_s \dot{\varepsilon}_{xx}$$
 (B1)

The shear-stress component,  $\tau_{xy}$ , is reduced to influence of Couette flow in the subduction channel. This is initiated by the difference in the north-south motions across the subduction zone,  $V_y$  (Fig. B2 a,b). The shear stress in the channel is therefore:

$$\tau_{xv} = \mu_s V_v / h$$

In this expression we ignore the stresses associated with variations of velocity  $V_x$  in north-south direction,  $\partial V_x / \partial y$ . In the assumptions of our simplified estimations (preferable deformation of the subduction channel) this type of deformation results in rotation of stronger parts and corresponding Couette flow in the channel, which in turn results in stresses of the same order as already estimated. Integration and simplification  $(\dot{\varepsilon}_{xy} \approx V_y / D/2)$  yield the expression:

$$\overline{\tau}_{xy} = 2\Delta D\mu_s \dot{\varepsilon}_{xy}$$
 (B2)

The yy component of the stress tensor is caused by north-south variations in the north-south velocity,  $V_y$  (Fig. B2 c and d). The corresponding component of the strain-rate tensor is  $\dot{\mathcal{E}}_{yy} = \partial V_y / \partial y \approx V_y / D_y$ , where  $D_y$  is the size of the subduction zone element in the Y direction. The strength of the subduction zone element in this direction is limited by the strength of the competent layers as the deformation cannot be limited to subduction channel only:

$$\tau_{yy} = 2\mu_c V_y / D_y$$
  
$$\overline{\tau}_{yy} = 2\mu_a L_s \dot{\varepsilon}_{yy}$$
(B3)

where  $\mu_a$  is an average viscosity in the subduction zone, and should be limited by values of viscosity of the strong parts of the zone,  $\mu_c$  and  $\mu_o$ . Summarizing equations B1 – B3, we obtain the following relation for the anisotropic rheology of the subduction zone elements:

$$\begin{pmatrix} \overline{\tau}_{xx} \\ \overline{\tau}_{yy} \\ \overline{\tau}_{xy} \end{pmatrix} = 2 \begin{bmatrix} \Delta^3 D \mu_s & 0 & 0 \\ 0 & L_s \mu_a & 0 \\ 0 & 0 & \Delta D \mu_s \end{bmatrix} \bullet \begin{pmatrix} \dot{\varepsilon}_{xx} \\ \dot{\varepsilon}_{yy} \\ \dot{\varepsilon}_{xy} \end{pmatrix} \approx 2 L_s \begin{bmatrix} \Delta^3 \mu_s & 0 & 0 \\ 0 & \mu_a & 0 \\ 0 & 0 & \Delta \mu_s \end{bmatrix} \bullet \begin{pmatrix} \dot{\varepsilon}_{xx} \\ \dot{\varepsilon}_{yy} \\ \dot{\varepsilon}_{xy} \end{pmatrix}$$
(B4)

The approximate derivations of this section aimed to give the qualitative conclusion that averaged over lithospheric thickness subduction zone behaves anisotropically. Moreover, the parameters of equation B4 are difficult to obtain in nature, so we use a simplified version of equation B4 (see eq. 4) in our calculations. The analysis presented here, however, can conclude that the viscosity associated with the shear stress component is smaller than one associated with  $\tau_{xx}$ , because  $\Delta >>1$ . The above analysis cannot estimate the difference in strength of subduction zone in x and y directions, because the components of viscosity in these directions involve  $\Delta >>1$  and  $\mu_a >>\mu_s$  and we leave this analysis to numerical experiments.

Variable	Description	Value in reference
		model
8	Acceleration due to gravity	$9.8 \text{ m/c}^2$
$ ho_m$	Density of mantle lithosphere	$3.3 \times 10^3 \text{ kg/m}^3$
$\Phi$	Isostatic amplification factor	$1-\rho/\rho_m$
Oceanic pl	late	
$\mu_o$	Characteristic viscosity of lithosphere	$2 \times 10^{24}$ Pa·s
$L_o$	Characteristic thickness of lithosphere	50 km
ρ	Density of oceanic crust	$3 \times 10^3$ kg/m <sup>3</sup>
Subduction	n zone	
$\mu_{xx}$	Viscosity of the subduction zone in the <i>X</i> (east-west) direction	$3 \times 10^{20}$ Pa·s
$\mu_{vv}$	Viscosity of the subduction zone in the <i>Y</i> (north-south) direction	$7 \times 10^{22}$ Pa·s
$\mu_{xy}$	Viscosity of the subduction zone in a simple shear	$10^{19}$ Pa·s
$L_s$	Characteristic thickness of the lithosphere in the vicinity of the	100 km
	subduction zone	
Continenta	ıl plate	
$\mu_{c0}$	Characteristic viscosity of undeformed foreland lithosphere	$7 \times 10^{22}$ Pa·s
$\mu_{cl}$	Characteristic viscosity of orogenic lithosphere	$2.8 \times 10^{21}$ Pa·s
$L_c$	Characteristic thickness of lithosphere	100 km
ρ	Density of crust	$2.8 \times 10^3 \text{ kg/m}^3$
$H_0$	Thickness of undeformed crust	39 km
$H^*$	Critical thickness of crust for channel flow	62 km
Mid to low	per crustal channel	
h	Thickness of the channel	10 km
$\mu_{ch}$	Viscosity of the channel rock (changes at critical thickness of the	$10^{20}/10^{22}$ Pa·s
	crust, H*)	
Character	istic ratios of the model	
$\overline{\mu}_{c1}/\overline{\mu}_{c0}$	Strength of the orogenic lithosphere relative to the strength of the	0.04
	foreland lithosphere	
$\overline{\mu}_{xx}$ / $\overline{\mu}_{c1}$	Strength of the subduction zone relative to the strength of the orogenic	0.11
	Andean lithosphere	
$R_{c/s}$	Relative strength of the subduction zone at 19°S and at 32°S	1

Table 1. Parameters of the model

# **Figure captions**

- Figure 1. Topography and bathymetry of the adjoining Nazca and South American plates. Plate boundary (thick black line), coastal line (white line), 3 km elevation line (thin black line), Atacama Basin (AB), Altiplano and Puna plateaus, Arica bend (AR).
- Figure 2. Subduction zone (above) and subduction zone element (below) described in the text. See Appendix B for integrated rheology of the subduction zone element.
- Figure 3. Schematic diagram illustrating inferred changes in the strength envelope of the continental lithosphere during orogenesis: (a) Initial strength of the lithosphere  $\overline{\sigma}_0$ ; (b) Strength  $\sigma_1$  after sudden thickening of the lithosphere (dashed line). Thermal relaxation weakens the lithosphere to  $\sigma_2$  (solid line); (c) Strength  $\sigma_3$  after weakening due to heat advected from the asthenosphere. Note that partial melting in the lower crust does not significantly decrease the integrated strength of the lithosphere.
- Figure 4. Plot of integrated viscosity of the continental lithosphere versus thickness of the continental crust for different ratios (1, 0.5 and 0.04) of the integrated viscosities of the continental foreland ( $\overline{\mu}_{c0}$ ) and orogenic lithosphere ( $\overline{\mu}_{c1}$ ).  $H_0$  and  $H^*$  are the characteristic thicknesses of the crust in the continental foreland and in the orogen, respectively. Circles indicate values obtained from the reference model of Sobolev et al. (this volume): solid circle = strength of the western margin of the Brazilian shield, open circles = strength of the orogenic crust.
- Figure 5. Areal distribution of directional integrated viscosity for different shear configurations in the reference model: (a) pure shear in an east-west direction or simple shear in a north-south direction; (b) pure shear in a north-south direction. The viscosity of the oceanic plate,  $\overline{\mu}_{c1}$ , is isotropic and depends on the age of the oceanic lithosphere. Likewise, the viscosity of the continental lithosphere,  $\overline{\mu}_c$ , is isotropic but depends strongly on crustal thickness. The strength of the subduction zone is anisotropic (eq. 4). The values of integrated viscosity in this diagram are the integrated viscosity normalized to the viscosity of a characteristic lithosphere (thickness  $L^*=100$  km, average viscosity  $\mu^*=10^{23}$  Pa·s). Map symbols as in Fig. 1.
- Figure 6. Deformation of the upper plate in a subduction orogen: (a) initial configuration; (b) tectonic thickening; (c) gravity spreading; (d) channel flow creating a plateau. Black arrows illustrate forces acting on the orogenic system, white arrows indicate material flow.
- Figure 7. General relationship between the lower crustal channel and the orogenic plateau: (a) General view of the plateau margin with different locations for the edge of the low-viscosity channel. GCC = channel with its edge directly below the plateau margin at a critical depth, D\*. OC = channel with its edge at a depth less than the critical value needed for sustaining a plateau. UC = channel with its edge beneath the plateau. OC and UC are inconsistent with topography; (b) Variation of flux along the three types of channel; (c) Average flux in the channel versus depth of the channel edge.
- Figure 8. Average flux in channels for different values of critical crustal thickness, H\*. Comparison with Fig. 7c indicates that the most suitable value of H\* is 62 km, corresponding to a plateau elevation of 3.5 km.
- Figure 9. Rates of thickness change in the reference model due to different modes of orogenic deformation (as in Fig. 6): (a) tectonic thickening; (b) gravity spreading; (c) channel flow; (d) all modes simultaneously.
- Figure 10. Distribution of westward velocity (a) and rate of the horizontal shortening along the Andean chain (b) in the reference model.
- Figure 11. Distribution of south-north flow in the crust (a, northward flow is positive) and vorticity (b) in the reference model.

- Figure 12. Plot of relative strengths showing the range of strength ratios in the model (area shaded grey) that yield deformational rates that are consistent with observed values in the Andes. The lines delimiting this domain represent bounds on the observed shortening rates. Solid lines: 1-1.75 cm/y for the central Andes (18-20°S), dashed lines: 0-0.5 cm/y for the southern Andes (30-32°S), dotted line: > 0.9 cm/y for the difference in shortening rates between the central and southern Andes. Rectangle refers to ratios in our reference model.
- Figure 13. Plot of relative strengths with domains of strength ratios (shaded grey) that yield realistic Andean deformational rates for three different values of  $R_{c/s}$  (1, 2 and 5).  $R_{c/s}$  describes the along-strike gradient in the strength of the subduction zone between the Nazca and South American plates. This strength decreases linearly along strike of the plate margin from  $\overline{\mu}_{xx}$  at 19°S to  $\overline{\mu}_{xx}/R_{c/s}$  at 32°S.

The same along-strike gradient is assumed for the subduction zone to the north of 19°S. The lines delimiting the shaded domains are the same as in Fig. 12, except that results for  $R_{c/s} = 5$  are limited by the additional constraint that deformation of the Brazilian shield is insignificant. The rectangle refers to ratios in our reference model, the circle refers to ratios in the models of Sobolev et al. (this volume).

- Figure B1. Estimates of the integrated normal stress due to variations in velocity,  $V_x$ , in the X-direction within the subduction zone: (a) general view; (b) break down of  $V_x$  into velocities parallel and normal to the subduction channel; (c) and (d) flow in the channel at velocity  $V_x$  tangential and normal to the channel boundaries, respectively.
- Figure B2. Estimates of the integrated normal stresses in the subduction zone due to variations in velocity,  $V_y$ , in the X-direction (a general view, b associated flow), and in the Y-direction (c general view, d associated flow).



Fig 1.



Fig 2.



Fig 3.



Fig 4.



Fig 5.



Fig 6.



**Fig 7.** 



Fig 8.



Fig 9.



Fig 10.



Fig 11.



Fig 12.



Fig 13.



Fig B1.



Fig B2.